

(12) INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

(19) World Intellectual Property Organization
International Bureau



(43) International Publication Date
7 December 2000 (07.12.2000)

PCT

(10) International Publication Number
WO 00/74264 A1

(51) International Patent Classification⁷: **H04B 7/02**,
H04L 27/06

(21) International Application Number: **PCT/US00/12069**

(22) International Filing Date: **3 May 2000 (03.05.2000)**

(25) Filing Language: **English**

(26) Publication Language: **English**

(30) Priority Data:
60/136,699 28 May 1999 (28.05.1999) US
09/378,337 20 August 1999 (20.08.1999) US

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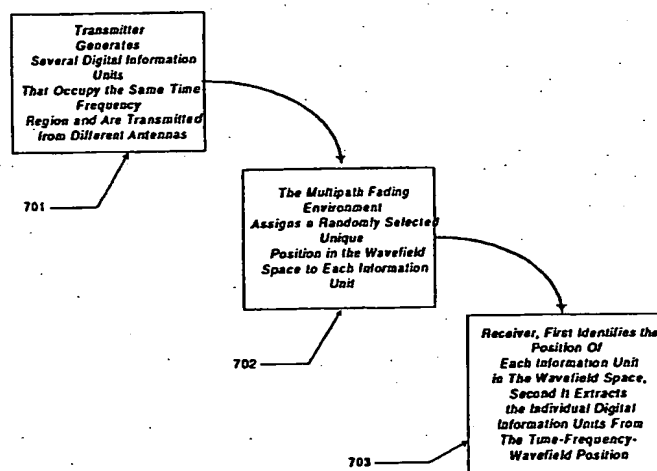
(81) Designated States (*national*): AE, AG, AL, AM, AT, AU,
AZ, BA, BB, BG, BR, BY, CA, CH, CN, CR, CU, CZ, DE,
DK, DM, DZ, EE, ES, FI, GB, GD, GE, GH, GM, HR, HU,
ID, IL, IN, IS, JP, KE, KG, KP, KR, KZ, LC, LK, LR, LS,
LT, LU, LV, MA, MD, MG, MK, MN, MW, MX, NO, NZ,
PL, PT, RO, RU, SD, SE, SG, SI, SK, SL, TJ, TM, TR, TT,
TZ, UA, UG, UZ, VN, YU, ZA, ZW.

(84) Designated States (*regional*): ARIPO patent (GH, GM,
KE, LS, MW, SD, SL, SZ, TZ, UG, ZW), Eurasian patent
(AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European patent
(AT, BE, CH, CY, DE, DK, ES, FI, FR, GB, GR, IE, IT, LU,
MC, NL, PT, SE), OAPI patent (BF, BJ, CF, CG, CI, CM,
GA, GN, GW, ML, MR, NE, SN, TD, TG).

Published:
— With international search report.

For two-letter codes and other abbreviations, refer to the "Guid-
ance Notes on Codes and Abbreviations" appearing at the begin-
ning of each regular issue of the PCT Gazette.

(54) Title: **METHOD AND APPARATUS FOR HIGH DATA RATE WIRELESS COMMUNICATIONS OVER WAVEFIELD SPACES**



(57) Abstract: The invention relates to a method and apparatus for digital communications (fig. 2) that provides high data rate wireless connections with bandwidth efficiency. The creation of multiple channels between the transmitter (701) and the receiver (703) is achieved by sampling the wavefield space with respect to the spatial domain. At the transmitter (701), symbols are simultaneously modulated and transmitted using signals that occupy the same frequency portion of the spectrum, but are distinguishable because different is their position in the wavefield space. The received signals are optimally processed to extract the digital information. Given a perfect estimate of the wavefield space parameters, the Maximum Likelihood principle is the optimum strategy for detection. When the wavefield space parameters are a-priori unknown, the Maximum Likelihood detector can not be implemented.

WO 00/74264 A1

METHOD AND APPARATUS FOR HIGH DATA RATE WIRELESS COMMUNICATIONS OVER WAVEFIELD SPACES

REFERENCE TO RELATED APPLICATIONS

This application claims priority to Provisional Application No. 60/136,699,
5 filed on May 28, 1999, incorporated herein by reference.

FIELD

The invention is directed to a method and apparatus for high data rate wireless
communications over wavefield spaces. In particular, the invention provides a high
data rate wireless communication between transceivers using a multi-dimensional
10 technique.

BACKGROUND

The wireless communication industry is responding to consumer demand for
high speed data services. The increased Radio Frequency (RF) spectrum acquisition
costs associated with the achievement of throughputs that are comparable with wired
15 communication technology has dramatically enhanced the interest in new methods to
obtain spectrally efficient modulation formats. The technical challenge posed by these
emerging requirements is residing in the intrinsic physical limitations of the wireless
propagation environment. Noise, interference, severe multipath and time-varying
characteristics of the fading channel contribute to make high-speed wireless data
20 communications a difficult and challenging problem. Traditional communication
engineering theory states that an increase in data rate is achieved by a combination of
an increase in bandwidth occupation, an increase in radiated power at the transmitter,

and an increase in dimensionality in the signal space (that is the order of the digital modulation). A greater description of the prior art and background is provided in Appendix 1 of Provisional Application No. 60/136,699, filed on May 28, 1999 incorporated herein by reference.

5 Conventional communication technology is depicted in Figures 1A-B. A communication network between transceiver A and transceiver B employs a two-dimensional communication protocol using time and frequency. The message to be communicated is broken into a plurality of smaller messages, or packets, that can be sent in the various time slots and frequency slots, according to the communication
10 protocol. Since the receiver knows the communication protocol, it can reassemble the packets to replicate the original message. This type of communication protocol is well known in the art. A greater description of the prior art and background is provided in Appendix 1 of Provisional Application No. 60/136,699, filed on May 28, 1999 incorporated herein by reference.

15 What is needed is a communication system that provides high data rate communication in a wireless environment. The present invention analyzes practical methods to demodulate high data rate signals transmitted from different positions (antenna elements), that are afflicted by arbitrarily time-varying fading characteristics, with arbitrary time dispersion (frequency selective fading). This is of significant
20 practical interest because in practice the fading environment can never be considered perfectly static even if transmitter and receiver are not in relative motion. The presented method and apparatus do not need training sequences or signals to estimate the channel: this gives additional advantage in terms of throughput with respect to prior art. The method and apparatus is implemented using available hardware for
25 digital radio transceivers.

SUMMARY

The invention overcomes the conventional limitations and provides a high data rate wireless communication system between transceivers using a multi-dimensional technique. An exemplary embodiment of the invention for communicating
30 information from one location to another through a wavefield space using a multi-dimensional communication protocol comprises a transmitter configured to receive a message and to encode a plurality of signals associated with the message. A first

plurality of antennas is coupled to the transmitter and configured to transmit the plurality of signals associated with the message into the wavefield space. A second plurality of antennas is configured to receive the plurality of signals associated with the message. A receiver is coupled to the second plurality of antennas and configured to decode the plurality of signals associated with the message, wherein the receiver has no advance knowledge of at least one of the dimensions of the multi-dimensional protocol. The receiver reconstructs the message to retrieve the original information.

In one aspect of this embodiment, the multi-dimensional protocol is at least a three-dimensional protocol and the transmitter includes a plurality of transmit modules that each encode at least a portion of the message. The receiver includes a plurality of receiver modules that each decode complementary portions of the message to reconstruct the original information.

In another embodiment, the receiver is configured to execute a statistical procedure to identify and decode the plurality of signals. In one aspect of this embodiment, the receiver is configured to execute a Generalized Likelihood Detection (GLD) procedure to identify the plurality of signals and then execute a Maximum Likelihood Detection procedure (MLD) to decode the plurality of signals. In another aspect of this embodiment, the receiver is configured to estimate the wavefield space using a virtual wavefield space that approximates the wavefield space.

In yet another embodiment of a digital wireless transceiver, the transceiver comprises a digital circuit for detection of U number of different signals after radio frequency intermediate frequency downconversion comprised of digital baseband downconversion, trellis search processor, vector symbol synchronizer, wavefield estimator, wavefield gradient-based estimator, deinterleaver, channel decoder and data extractor; and a digital circuit for detection of U number of different signals after radio frequency intermediate frequency downconversion able to cope with and exploit frequency selective multipath propagation, arbitrarily time-varying fading characteristics, non Line-Of-Sight communication.

Advantages of the invention include the ability to communicate high data rates from one location to another, where the data rates are in excess of those conventionally achievable.

BRIEF DESCRIPTION OF THE FIGURES

Figures 1A-B depict conventional communication technology according to the prior art;

Figures 2A-B depict communication technology and a three-dimensional communication protocol according to an embodiment of the invention;

Figure 3 is a flowchart depicting a sequence of events characterizing a communication protocol between two wavefield transceivers according to an embodiment of the invention;

Figure 4 illustrates the preferred embodiment of the invention in a transceiver (that is an apparatus for transmission and reception of digital information over the wavefield space);

Figure 5 illustrates in more detail the Radio Frequency (RF) section of the transceiver

with Analog to Digital and Digital to Analog conversions;

Figure 6 illustrates in more detail the Digital Signal Processing section of the Receiver;

Figure 7 illustrates in more detail the Digital Signal Processing section of the Transmitter; and

Figure 8 is a flowchart procedure to find the optimum P and M.

DETAILED DESCRIPTION

The detailed description of the invention is organized in subsections where each subsection explains a topic that is fundamental to explain and justify the methods and associated apparatus. This description incorporates Appendix 1 of Provisional Application No. 60/136,699, filed on May 28, 1999 herein by reference.

A. Introduction

The present invention provides high data rate communication between a plurality of base stations where each base station transmits, using a plurality of antennas, into a multi-path wavefield space. The signals are received by selected base station and resolved and decoded to recover the original transmitted information.

The wavefield space is the space spanned by the channel parameters that characterize the multipath fading environment. The communication involves sampling

the wavefield space. Sampling the wavefield space creates a multi-link connection resource between the transmitter and the receiver. One aspect of the invention involves the spatial sampling of the wavefield space by antennas. As the transmitter symbols are modulated and simultaneously transmitted using signals that occupy the same frequency portion of the spectrum, they are distinguishable because of their different positions in the wavefield space. The shape of the wavefield space depends on the particular propagation environment. The optimum demodulator is a device that estimates the wavefield space parameters and performs optimum separation of the different signals to obtain the multiple streams. Evidently, the throughput of such a communication system is an integer multiple of the throughput that is achievable at each different position in the wavefield space. The concept of wavefield modulation can be better understood with reference to Figures 1 and 2, showing the transfer of digital information units from the baseband digital signal processing (DSP) domain to the Radio Frequency domain and vice versa. Figure 1 depicts the conceptual operation performed by a traditional transceiver (that is a transmitter-receiver apparatus based on prior art). The baseband DSP processors 507 generate digital information units (packets) 503 in a non-synchronous fashion. The traditional transceiver 506 is responsible for modulating such digital information units (packets) 503 and allocate 504 each unit (packet) in a preassigned position in the time-frequency two-dimensional space: one point in the time-frequency plane corresponds to a signal that exist in a particular time instant given by the projection of the point onto the time axis 501 and with an instantaneous frequency given by the projection of the point onto the frequency axis 502. The traditional transceiver 506 is also responsible for demodulating such digital information units (packets) 503, extract 505 each unit (packet) from a preassigned position in the time-frequency two-dimensional space, and route the units 503 to the baseband DSP processors 507. The traditional transceivers are limited in throughput by the number of available slots in the time-frequency two-dimensional space since no two signals can occupy the same position in the space.

In contrast, the wavefield transceiver 506 shown in Figure 6 is capable of much higher throughput given the same number of slots in the time-frequency two-dimensional space since, in fact, two signals can occupy the same position in the space. The basic mechanism that allows this is the fact that the wavefield transceiver 506 is capable of enabling the allocation of digital information units (packets) 503 in a

third dimension 601, which is defined as the wavefield space. Basically, the throughput is now limited by a three-dimensional volume instead of the traditional two-dimensional volume. The wavefield transceiver 506 enables the allocation 504 (or extraction 505) of digital information units (packets) 503 in the wavefield space by transmitting (and receiving) from different points in space that exploits the multipath propagation environment for communicating across new dimensions. Figure 3 describes the fundamental sequence of events 701, 702, 703 that characterize a communication session between two wavefield transceivers.

Given a perfect estimate of the wavefield space parameters, the Maximum Likelihood principle is the optimum strategy for detection. When the wavefield space parameters are not known in advance, the Maximum Likelihood detector can not be immediately implemented. A typical approach is the Generalized Likelihood Detector (GLD), which uses a Generalized Likelihood statistic (GLS) to detect the signals. The Generalized Likelihood statistic, derived for time-varying wavefield spaces, involves finding the orthogonal projection of the received signal onto the signal subspace; the transmitted signal (corresponding to one of the transmitted sequences of symbols) is known to lie in a subspace but its exact location is not known because the wavefield space parameters are unknown. Detectors in this class are also used in signal processing because their statistic is "matched" to the a-priori known signal subspace S. The (perfectly matched) orthogonal projection of the received signal onto the signal subspace S is difficult (if not impossible) to compute. To estimate the subspace S, the invention employs virtual subspaces, say V, that approximate the original signal subspace S in some sense, and whose orthogonal projections are more easily computed. These reduced-size signal subspaces V are obtained by a decomposition of the fading channel time variations using orthonormal wavelet bases.

The merits of the wavelet decomposition are to be reconducted to an outstanding localization capability in the time-frequency plane. Using expansions for a generic signal by means of orthonormal functions that are well-localized in the time-frequency plane implies that only a few coefficients of the expansion can be adopted to represent with extreme accuracy the original signal. Basically, the method and resulting apparatus use an efficient representation of the fading statistics in the maximum likelihood formulation of the detection problem.

In fact, the set of linear vector spaces defined by such decomposition provides also a nested sequence of subspaces that, at increasing level of detail, are "efficient" representations of the original signal subspace S. Part of the invention is a method to "focus" these (subspace) representations to the original signal subspace using the concept of Kolmogorov n width for signal classes. The use of the focused wavelet-based model in the statistic of the detector results in an effective approach to wavefield space demodulation.

B. Exemplary Transceiver

The basis for the present invention is communication between a plurality of base stations where each base station transmits, using a plurality of antennas, into a wavefield space. The signals are received by a selected base station and resolved and decoded to recover the transmitted information. The invention is performed by a base station structure similar to that described in U.S. Pat. No. 5,678,268, assigned to the same assignee as this application and incorporated herein by reference.

Wideband Radios use a single Radio Frequency path to access the entire allocated band, performing traffic channelization via digital signal processing. Traditional radios perform traffic channelization in hardware and typically require an additional hardware combining network for multi-channel systems. The flexibility increase inherent to wideband stems from the fact that the channelization process can be done in software or reconfigurable logic which can not only be upgraded but could be dynamically changed on a connection by connection basis as described in U.S. Pat. No. 5,678,268. Figure 4 shows a Wideband architecture for a transceiver (that is an apparatus able to transmit and receive exploiting the wavefield modulation previously described). A plurality of receiving antennas 100 are connected to the site RF distribution 111 which is a network of RF signal distribution circuits. The Power Amplifiers 101 are necessary to amplify the transmit signal to reach the remote receiver at adequate distance. The Wideband Receiver Modules 102 (one per antenna) are in charge of filtering, amplifying, downconverting and digitizing the RF spectrum of interest. The digital samples at the output of the ADC from each of the Wideband Receiver Modules 102 are routed appropriately time-multiplexed to the Wideband Digitized Spectrum Data Distribution 108. Digital Receiver Processing modules 105

perform traffic channelization, demodulation and data extraction. On the transmit path the digital transmitter 106, the Wideband Exciter 103 perform the reverse operations.

The Wideband Receiver 102 and Exciter 103 RF Modules functional diagrams are illustrated in Figure 5. The wideband receiver 102 is designed to be driven from a site RF distribution 111 network and minimizes this interface requiring a single, low gain RF feed per antenna element. High dynamic range amplifiers 203 and mixers 206 are utilized to obtain a large instantaneous dynamic range, thus preserving signal fidelity. The signal as collected by the antenna 100 is filtered 202, amplified 203, further filtered 203 and amplified 204. It is then mixed 206 by a first Local Oscillator 209 and filtered 207, amplified 203 and mixed down 206 to intermediate frequency by a second Local Oscillator 209. A filter 208 removes unwanted high frequency components and the resulting signal is further amplified 203 before being injected to the analog to digital converter 210. The clock to the analog to digital converter 210 is generated by a frequency source 209 locked to the site frequency reference 109. The samples at the output of the Analog to Digital Converter are routed to the 108 Wideband Data Distribution Bus. This Bus 108 is a high speed Time Division Multiplexed resource that connects any RF module to any Digital receiver module in a non-blocking fashion. All frequency and clock conversion oscillators are locked to the external site frequency reference 109 ensuring coherent operation. The Wideband Exciter 103 RF Module is also illustrated in Figure 5. The samples from the 108 Wideband Data Distribution Bus are routed to the Digital to Analog Converter 212. The analog signal then is filtered 208, amplified 203 and mixed 206 using the second Local Oscillator 209 frequency. The RF signal is further filtered 207, amplified 203 and upconverted 206 using the first Local Oscillator 209 frequency. After proper amplification 203 and filtering 204 the signal goes to a multicarrier power amplifier that is responsible for providing enough RF power to the signal to reach the remote receiver after antenna radiation.

A block diagram for the Digital Receiver Module is shown in Figure 6. The traffic channelization (that is baseband conversion) is performed using digital quadrature downconversion implemented by means of specialized high-speed ASIC 301. The samples from the Wideband Digitized Data Distribution 108 are downconverted to baseband by means of a quadrature mixer 302 where the mixing frequency is generated by a NCO (Numerically Controlled Oscillator) 303. An NCO

is a digital implementation of what is known in the analog domain as Voltage Controlled Oscillator. The two branches (In-Phase and In-Quadrature) of the samples are filtered by filters 314 to remove high frequency components of the mixing process. Each of the digital downconverters is connected to pulse shaping filters 306 that are
5 matched to the transmitted pulse shapes and the output of these filters are sampled at a rate that is an integer multiple of the symbol rate. These samples are known to constitute a sufficient statistic for the trellis search 308 previously described. The synchronizer 307 is responsible for optimizing the sampling instants at the output of the shaping filter. Wavefield estimation 309 is performed iteratively using the
10 Generalized Likelihood method described and the gradient update technique 310. The processing function following the demodulation 305 are related to the channel coding section of the communication system and are well-known to those skilled in the art of digital communications. A deinterleaver with channel decoder function 311 follows the demodulator. Data extraction 312 refers to the organization of the information
15 bitstream in a way that is compatible with the particular application of the communication system.

The block diagram for the Digital Transmitter Module is shown in Figure 7. The data is first properly organized in a bitstream from the user packet data distribution bus 104 by means of the data extraction function 409. Then, the data is
20 properly encoded 408 and interleaved 407. The modulator 405 basically organizes the high-speed single bitstream in multiple lower speed bitstreams. These bitstreams are modulated according to the particular digital modulation format of interest (for example M-QAM or M-PSK) and routed to the pulse shaping filters 406. The device that follows is a digital up-converter 401 that translates to a first intermediate
25 frequency the baseband signal at the output of the pulse shaping filters. The digital upconverter is constituted by filters 404, mixers (multipliers) 402, a Numerically Controlled Oscillator 403 and an adder 411. The digital samples at the output of the digital upconverter are routed by means of the Wideband Digitized Spectrum Data Distribution Bus 108 to the respective Wideband Exciter RF module 103 where they
30 are converted to analog signals and upconverted to RF.

Each module 102, 103, 105, 106 is controlled by a respective microcontroller 215, 216, 313, 410, each of which also provides an interface with the data distribution resources (Wideband Digitized Spectrum Data Distribution 108 and User Data

Distribution 104). Multiple modules can be replicated to meet traffic capacity and/or multiple antenna requirements.

C. Detailed Description of the Signal Processing Problem

Consider the communication between two base-stations where the transmit base-station has U antennas and the receive base-station is equipped with K antennas. At each antenna a different symbol stream is transmitted, so that the rate at which symbols are transmitted by the U-antenna transmitter is U times the rate at any single antenna.

It will be immediately evident to those skilled in the art of wireless receiver technology that the effect of a time-varying multipath channel can be represented at baseband (at the output of the pulse shaping filters 306 in Figure 6) using the complex sequence of samples

$$y_k(n) = a(n)^T h_k(n) + \eta_k(n), \quad n=0,1,2,\dots,RN-1, \quad k=1,2,\dots,K \quad (1)$$

where T means transpose for vectors or matrices,

$$a(n) = [a_1(n), \dots, a_1(n-D), a_2(n), \dots, a_2(n-D), \dots, a_U(n), \dots, a_U(n-D)]^T$$

is a vector that contains the N symbols transmitted by each of the U antennas interlaced (or zero-padded) with R-1 zeros and

$$h_k(n) = [g_{k,1}(n,0), g_{k,1}(n,1), \dots, g_{k,1}(n,D), g_{k,2}(n,0), g_{k,2}(n,1), \dots, g_{k,2}(n,D), \dots, g_{k,U}(n,0), \dots, g_{k,U}(n,D)]^T.$$

is a vector of complex samples that contains the baseband discrete-time impulse responses from any of the U transmit antennas to the kth receive antenna. The generic element $g_{k,l}(n,m)$ of $h_k(n)$ represents the response of

1. pulse shaping at the lth transmit antenna;
2. transmit RF filters at the lth transmit antenna;
3. mth tap of the discrete time multipath impulse response at time n between lth transmit antenna and kth receive antenna;

4. receive RF filters at the kth receive antenna; and
5. pulse shaping at the I-th transmit antenna.

D is an integer that characterizes the length of the finite impulse response (FIR) $g_{k,l}(n,m)$ between any of the U transmit antennas to any of the K receive antennas. The index n simply describes the fact that such impulse responses are time-varying. The complex scalar $\eta_k(n)$ represents additive White Gaussian Noise afflicting the observation at the kth receive antenna.

More details regarding this technique of modeling multipath can be found in M. Martone, "An adaptive algorithm for adaptive antenna array low-rank processing in cellular TDMA base-stations," IEEE Trans. Commun., vol. 46, pp. 627-643, May 1998; M. Martone, "On MMSE Real-Time Antenna Array Processing Using Fourth-Order Statistics in the US Cellular TDMA System," IEEE Journal Sel. Areas in Comm., vol. 16, N. 8, pp. 1396-1410, Oct. 98; and M. Martone, "Cumulant-based adaptive multi-channel filtering for wireless communication systems with multipath RF propagation using antenna arrays" IEEE Trans. Veh. Tech., Vol. 47, no. 2, pp. 377-391 May 98.

The samples $y_k(n)$ are samples of the baseband signal collected at the kth antenna at sampling rate equal to R/T if we denote $1/T$ as the rate at which the U antennas transmit synchronous symbols. More explicitly

1. $a_i(n)$ is a complex number representing a point (symbol) in the constellation if n is equal to 0, R, 2R, 3R, ..., NR; and
2. $a_i(n)$ is equal to zero if n is not equal to 0, R, 2R, 3R, ..., NR.

The integer parameter R is the so called oversampling factor and it represents the number of signal samples that are contained in one symbol period T. It is well-known that $R=1$ is sufficient for optimum detection. However in a practical receiver $R>1$ makes implementation more robust with respect to synchronization issues. It is important to remind that in the model at hand for $K=1$, $L=1$, $R=1$ and static channel, that is $g_{k,l}(n,m) = g_{1,1}(m) = g(m)$ for any n, equation (1) collapses into the well-known model for reception of digital signals in presence of Intersymbol Interference (see J. G. Proakis, "Digital communications," McGraw-Hill, Third Edition, 1995).

$$y_1(n) = \sum_m g(m) a_1(n-m) + \eta_1(n), \quad n=0,1,2,\dots,RN-1 \quad (2)$$

Equation (2) represents an unrealistic model in real life wireless communication channels and much more importantly the communication system modeled by equation (2) has a maximum throughput of N symbols per NT seconds, while equation (1) is representative of a communication system where the throughput is UN symbols per
 5 NT seconds.

The task of the receiver base-station signal processing is to obtain an estimate of the vector of symbols $a(n)$ for $n=0,1,\dots, NR-1$, (in other words an estimate of the sequence $a=[a(0)^T, a(1)^T, \dots, a(NR-1)^T]^T$), given only the received samples $y_k(n)$.

If the communication system uses Q-ary symbols then the vector a can be any of
 10 Q^{UN} different vectors. We identify the hypothetical vector as $s=[s(0)^T, s(1)^T, \dots, s(NR-1)^T]^T$.

The Maximum Likelihood formulation of the detection/estimation problem can be stated as in the following:

15 Find the minimum of

$$L_N[s] = \sum_{k=1,2,\dots,K} \sum_{n=0,1,\dots,NR-1} |y_k(n) - s(n)^T h_k(n)|^2$$

over "any possible"

$$s = [s(0)^T, s(1)^T, \dots, s(NR-1)^T]^T$$

Observe that "any possible" refers in the above formulation to the fact that since
 20 the elements of s are symbols that can assume only a finite number of values (the Alphabet of the digital modulation method of choice), there will also be only a finite number of vectors s . Also, one of the many $s=[s(0)^T, s(1)^T, \dots, s(NR-1)^T]^T$ is indeed the transmitted one vector $a=[a(0)^T, a(1)^T, \dots, a(NR-1)^T]^T$.

However the big practical problem in this optimum formulation of the problem is
 25 that the receiver does not know the multipath channel parameters (the wavefield parameters). Prior art has solved this problem sending training sequences of known symbols that allow channel estimation. This technique has two drawbacks:

1. it works only for static channels (that is non-time varying); and
2. it dramatically reduces the throughput of the system because of the periodical
 30 training.

The first modification is to formulate the problem differently as in the following:

Find the minimum of

$$L_N[s] = \sum_{k=1,2,\dots,K} \sum_{n=0,1,\dots,NR-1} |y_k(n) - s(n)^T h_k(n)|^2$$

over "any possible"

$$s = [s(0)^T, s(1)^T, \dots, s(NR-1)^T]^T$$

5 and over $h_k(n)$.

This problem is solved in two stages:

Step 1: For any possible s find the Maximum Likelihood Estimate of $h_k(n)$, call it $h_k[s, n]$,

Step 2: Find the minimum of $L_N[s] = \sum_{k=1,2,\dots,K} \sum_{n=0,1,\dots,NR-1} |y_k(n) - s(n)^T h_k[s, n]|^2$
 10 over any possible s .

This two-step particular solution of the problem is called Generalized Likelihood solution (see L. Van Trees, "Detection, Estimation, and Modulation Theory" Part I, John Wiley 1968). Unfortunately this way of solving the detection problem still places a formidable computational challenge, essentially because a large number of
 15 free parameters are contained in $h_k(n)$, for any n and any k . In fact $h_k(n)$ is a non-parsimonious (in other words it has significant redundancy) representation of the wavefield multipath propagation environment. To minimize the amount of redundancy in $h_k(n)$ and get to the possible minimum number of parameters that truly characterize $h_k(n)$ especially as connected to our detection problem we use a wavelet
 20 orthonormal basis expansion of each element of $h_k(n)$, the wavefield response.

D. Multiresolution Decomposition of the Wavefield Multipath Response

An unknown deterministic or random signal can be decomposed according to its resolution (components at different levels). An excellent and very intuitive explanation of the concept of decomposing a signal at different resolutions is
 25 contained in the book "Wavelets and Filter Banks" by G. Strang and T. Nguyen, Wellesley-Cambridge Press, 1996.

The crucial point of almost all of the proposed methods for the detection of a signal of the form in (1) (even in the case of a single transmit antenna) is based on the assumption that the multipath channels are quasi-static, that is time invariant over the

length of the transmitted frame. Slow variations of the channels are then compensated by using adaptive algorithms that ultimately force the estimate to be constantly in search of a convergence point. If the channel coefficients variations in time are fast with respect to the convergence time of the adaptive algorithm, significant degradation may result. A more reasonable alternative is to model the time-varying components of the impulse response of the multipath channel as low-pass Gaussian processes with their correlation representing ensemble average characteristics. These average characteristics are in turn used to fit parametric models so that a bank of Kalman filters can be used for tracking. This approach is impractical because the parametric models that best fits the channel dynamics have a large number of free parameters. Moreover, the generalization of this approach to a multi-antenna environment where possibly multiple different channel responses have to be estimated/tracked, is definitely a formidable task in terms of computational effort.

This invention departs from these well-known and obvious approaches in search of new methods that more "economically" can characterize the time varying nature of the detection/estimation problem. A multiresolution representation of the fading process in each component of the channel response is introduced, elaborating some ideas of (J. Zhang and G. Walter, "A wavelet-based KL-like expansion for wide-sense stationary random processes" IEEE Transactions on Signal Processing, vol. 42, no. 7, pp. 1737-1745, July 1994); (R. W. Dijkerman and R.R. Mazumdar, "Wavelet representations of stochastic processes and multiresolution stochastic models" Transactions on Signal Processing, vol. 42, no. 7, pp. 1640-1652, July 1994), M. I. Doroslovacki and H. Fan, "Wavelet-based linear system modeling and adaptive filtering," Transactions on Signal Processing, vol. 44, no. 5, pp. 1156-1167, May 1996. The unknown channel time variations are in fact decomposed using optimal unconditional bases such as orthonormal wavelet bases.

It is extremely important to realize that modeling of linear systems by basis functions can turn a time-varying system identification problem into a time-invariant one. Essentially inspired by Fourier harmonic analysis ideas, simple exponential bases were used in G. B. Giannakis and C. Tepedelenlioglu, "Basis-expansion models and diversity techniques for blind identification and equalization of time-varying channels," Proceedings of the IEEE, vol. 86, no. 10, pp. 1969-1986, Oct. 1998.

The exponential basis function of a Fourier-like decomposition has infinite duration, so clearly any representation of a time-localized signal is not efficient and adequate. To connect this consideration with a simple and intuitive example, consider a signal made of two pure oscillations occurring at non-overlapping distinct time intervals.

The Fourier transform reveals the presence of the two tones, but with no localization in time, which forces a wrong representation for the signal. In other words, representations based on exponentials lack "parsimony." The time-varying reflections of electromagnetic waves caused by a moving transmitter (or receiver) are in nature very similar to a signal where multiple propagation modes are present at different times. To represent the frequency behavior of a signal locally in time, the signal should be analyzed by functions which are localized both in time and frequency, for instance, signals that are compactly supported in the time and frequency domains. In reality no function can be compactly supported simultaneously in time and frequency so the scientific community has directed intense research efforts in the development of functions with "good" time-frequency localization: wavelets are the best known tool for linear time-frequency analysis. An obvious solution to the time-localization problem of the Fourier analysis is to localize the tones in the Fourier representation by windowing several time-consecutive intervals of the analyzed signal. This is in fact the short-time Fourier transform which basically operates a partition (or "tiling") of the time-frequency plane in rectangles of equal area. Wavelets can offer a different and valuable compromise: the frequency localization is logarithmic in frequency. Looking at the time-frequency plane, this means that time localization gets finer at the highest frequencies. The wavelet transform replaces the Fourier transform's sinusoidal waves by a family of functions generated by translations and dilations of a single window called a wavelet. Complicated signals can be represented using only a few wavelet and scaling functions and statistical signal modeling and processing methods based on the wavelet transform are in most cases much more effective than classical time-domain or frequency-domain approaches.

We give a brief explanation of the main concept disclosed in this invention by using an oversimplified continuous time single antenna model. Consider a sequence of digital symbols collected in the vector \mathbf{a} , digitally modulated to form the signal waveform $x(\mathbf{t}, \mathbf{a})$.

The signal $x(t, a)$ is the input to $h(t, \tau)$ the time-varying impulse response of a multipath channel, as

$$y(t) = \int_{\tau=-\infty, t} h(t, \tau) x(\tau, a) d\tau.$$

Assume that the kernel $h(t, \tau)$ can be represented by an expansion of the form

$$h(t, \tau) = \sum_{I \in H} w_I(\tau) \Psi_I(t)$$

where $\{\Psi_I(t)\}_{I \in H}$ is a set of functions (wavelets) and $\{w_I(\tau)\}_{I \in H}$ are the (wavelet) coefficients of the expansion. Using this representation we can express $y(t)$ as

$$y(t) = \sum_{I \in H} \Psi_I(t) \int_{\tau=-\infty, t} w_I(t-\tau) x(\tau, a) d\tau = \sum_{I \in H} \Psi_I(t) x'_I(\tau, a)$$

where $x'_I(\tau, a) = \int_{\tau=-\infty, t} w_I(t-\tau) x(\tau, a) d\tau$. This representation can be economical if the set $\{\Psi_I(t)\}_{I \in H}$ contains a small number of functions. The multiplication $\Psi_I(t) x'_I(\tau, a)$ emphasizes the time selection of the input content and its frequency translations. Observe that $x'_I(\tau, a)$ for any I in the set H is the output of a time-invariant linear filtering operation: it is simply obtained filtering $x(a, t)$ by $w_I(t)$. Another interesting property of this representation is that it gives us the ability to select for any given time interval only those wavelet coefficients responses $w_I(t)$ that affect the output during the time interval of interest. The use of wavelet bases allows the selection of the subset in H which will model the local and global characteristics of the channel dynamics. A clear attempt of the engineering community to have a global characterization of the time-varying nature of a multipath propagation link is the well-known WSSUS (Wide Sense Stationary Uncorrelated Scattering) model (J. G. Proakis, "Digital communications," McGraw-Hill, Third Edition, 1995)). The WSSUS assumption is only an approximation of the real propagation mechanism in a dense multipath environment. Indeed $h(t, \tau)$ has smooth (low frequency) variations with occasional rapid changes that can not be possibly modeled as stationary. In particular a channel model which is uniquely based on ensemble average characteristics will inevitably lose local characteristics that are caused for example by rapid transitions and sudden changes of the impulse response dynamics (for example the mobile transmitter coming to a sudden stop), while the multiresolution model will retain such information in a few high resolution "detail" coefficients. The idea is that the wavelet-based representations can better model not only non-stationary but also stationary processes. We will however use the WSSUS model to tune our channel representation and to

eliminate gross redundancy: in other words second-order statistics will provide general guidelines on how to select the low-resolution coefficients. It is however understood that retaining only the low-resolution coefficients will not give us the kind of "parsimony" that we expect from a wavelet-based representation. To achieve this goal
 5 a few high resolution coefficients empirically selected will be maintained.

Going back to our original discrete-time problem, we would like to obtain a practical basis representation for the discrete-time channel $g_{i1,i2}(n,k)$ that is easily parameterized, it retains the essential features of the fading process and it characterizes these features using a small number of time-invariant coefficients. These requirements
 10 can be satisfied using a discrete-time wavelet series representation. The orthonormal expansion we will derive can be thought more properly as a multiscale sub-band decomposition using filterbanks of the sampled response of a multipath channel. We direct the interested reader to P. P. Vaidyanathan, "Multirate Systems and Filter Banks," Prentice Hall, 1993, and in particular to O. Rioul, "A discrete-time
 15 multiresolution theory," IEEE Transactions in Signal Processing, vol. 41, no. 8, pp. 2591-2606, Aug. 1993, where a "discrete-time" approach to multiresolution representations is described. To simplify notation consider $g(n,k)$ as the generic response for a generic set of indices $i1,i2$. It is fundamental to observe that $g(n,k)$ can be represented at lower resolution applying a half band low-pass filter having impulse
 20 response $c_0(n)$ followed by a down-sampling-by-two operation

$$\zeta_{1,m}(k) = \sum_j c_0(j) g(2m-j,k).$$

This equation represents a mapping from a vector space to itself. An added "detail" can be obtained by using a high-pass filter with impulse response $c_1(n)$, then again down-sampling by two

$$\xi_{1,m}(k) = \sum_j c_1(j) g(2m-j,k).$$

The filters $c_i(n)$, $i=0,1$ satisfy some regularity constraints and form an orthonormal set. If $c_i(n)$ (in the z-domain $C_i(z)$) for $i = 0,1$ is a dyadic perfect reconstruction filter bank (P. P. Vaidyanathan, "Multirate Systems and Filter Banks," Prentice Hall, 1993), one can think of $\zeta_{1,m}(k)$ and $\xi_{1,m}(k)$ as a decomposition of $g(n,k)$ onto a discrete time
 30 orthonormal basis with the following (perfect) reconstruction rule

$$g(n,k) = \sum_m \zeta_{1,m}(k) c_0(2m-n) + \sum_m \xi_{1,m} c_1(2m-n),$$

which is indeed a sum of orthogonal projections. Using the same filters $c_i(n)$, $i=0,1$, the decomposition could be performed again in lowpass and highpass down-sampled components, and then further the lowpass component split again, up to a desired
 5 “depth” or resolution, so that one can always “explode” the lowpass component resolution

$$\zeta_{j,m}(k) = \sum_m \zeta_{j+1,m}(k) c_0(2m-n) + \sum_m \xi_{j+1,m} c_1(2m-n)$$

For example consider the equation above for $j=1$ to get

$$\begin{aligned} g(n,k) &= \sum_m [\sum_m \zeta_{2,m}(k) c_0(2m'-m) + \sum_m \xi_{2,m}(k) c_1(2m'-m)] c_0(2m-n) \\ &\quad + \sum_m \xi_{1,m}(k) c_1(2m-n) \\ 10 \quad &= \sum_m \zeta_{2,m}(k) c_0^{(2)}(2^2 m-n) + \sum_{l=1,2} \sum_m \xi_{1,m}(k) c_1^{(l)}(2^1 m-n) \end{aligned}$$

where $c_0^{(2)}(n)$, $c_1^{(2)}(n)$ and $c_1^{(l)}(n)$, $l=1,2$ are filters obtained in the z -domain as

$$C_0^{(2)}(z) = C_0(z) C_0(z^2), \quad C_1^{(1)}(z) = C_1(z), \quad C_1^{(2)}(z) = C_1(z^2) C_0(z).$$

In the last equation we have used the Noble identity (P. P. Vaidyanathan,
 15 “Multirate Systems and Filter Banks,” Prentice Hall, 1993) which says that a downsampler by two, followed by a filter $F(z)$ is equivalent to the filter $F(z^2)$ followed by the downsampler by two.

We can think of the derived expansion for $g(n,k)$, as a decomposition of $g(n,k)$ onto a discrete time orthonormal basis at resolution level $P=2$. The method can be
 20 applied recursively to obtain at generic resolution depth P a filter bank with $P+1$ branches.

The channel parameter $g_{i1,i2}(n,k)$ at any fixed k can be considered a signal at resolution 0 with an associated signal subspace $V_0 = S$. Of course $g_{i1,i2}(n,k)$ for $i1=1,2,\dots, U$ and $i2=1,2,\dots, K$ and $n=0,1,\dots, NR-1$ spanning V_0 perfectly represents the

wavefield response, but it has high degree of redundancy and it complicates our detection problem.

The orthonormal basis $c_p^{(q)}(2^q m-n)$ for $p=0,1$ and $q=1,2,\dots,P$ can be used to decompose $g_{i1,i2}(n,k)$ at resolution P

$$5 \quad g_{i1,i2}(n,k) = \sum_{m=0,1,\dots,NR/2^{P-1}} \zeta_{P,m,i1,i2}(k) c_0^{(P)}(2^P m-n) \\ + \sum_{l=1,2,\dots,P} \sum_{m=0,1,\dots,NR/2^{l-1}} \xi_{l,m,i1,i2}(k) c_l^{(l)}(2^l m-n) \quad (3)$$

The smaller P the higher the resolution (is the highest resolution). So greater P means less redundancy in the wavefield response representation. The filters $c_i(n)$ for $i=0,1$ satisfy some regularity constraints, and form an orthonormal set: they are
10 defined as a dyadic perfect reconstruction filter bank ("Wavelets and Filter Banks" by G. Strang and T. Nguyen, Wellesley-Cambridge Press, 1996). We are not interested in the details of why these constraints are related to the discrete time wavelet transform, all we care is that $\zeta_{P,m,i1,i2}(k)$ and $\xi_{l,m,i1,i2}(k)$ are <low redundancy> representations of $g_{i1,i2}(n,k)$. Equation (3) can be rewritten in vector form as

$$15 \quad g_{i1,i2}(n,k) = c(P,n)^T w_{i1,i2}(P,k)$$

In particular, given a particular P we can truncate the second summation by considering that we can neglect the last $\sum_{n=1,\dots,M} NR 2^{-m}$ components of the vector $w_{i1,i2}(k)$ (because typically very close to zero in real life multipath channels) and of the vector $c(P,n)$ so we can obtain a parsimonious representation of the channel as

$$20 \quad h_k(n) = C(P,M) w_k(P,M) \quad (4)$$

where $C(P,M)$ is simply a matrix of vectors $c(P,n)^T$ where the last $\sum_{n=1,\dots,M} NR 2^{-m}$ have been eliminated and $w_k(P,M)$ is simply a long vector obtained by the concatenation of vectors $w_{i1,i2}(P,k)$ for $i1=1,2,\dots,U$ and $i2=1,2,\dots,K$ and $k=0,1,\dots,D$ where the last $\sum_{n=1,\dots,M} NR 2^{-m}$ have been eliminated also.

25 Now that we are equipped with the representation (4) of the wavefield response we go back to equation (1) and observe that we can write

$$y_k(n) = a(n)^T C(P,M) w_k(P,M) + \eta_k(n) = a(n)^T w_k(P,M) + \eta_k(n), \quad (5)$$

where we have indicated $a(n)^T = a(n)^T C(P,M)$.

Denote now $d(n)^T = s(n)^T C(P,M)$ and $d = [d(0)^T, d(1)^T, \dots, d(NR-1)^T]^T$, and reformulate the Generalized 2-step Likelihood problem as:

- 5 Step 1: For any possible d find the Maximum Likelihood Estimate $w_k(P,M)$, call it $w_k[P,M,d]$, and

Step 2: Find the minimum of $L_N[d] = \sum_{k=1,2,\dots,K} \sum_{n=0,1,\dots,NR-1} |y_k(n) - d(n)^T w_k[P,M,d]|^2$ over any possible d .

- 10 The problem is now in simple form because the Maximum Likelihood estimate of $w_k(P,M)$ given s is dramatically simplified by the fact that the wavefield response is characterized by a static vector $w_k(P,M)$.

E. Focusing the Generalized Energy Detector

This subsection describes a method to select the proper integer parameters M and P , given a certain accuracy of representation of the wavefield space.

- 15 Described above is the practice that a multiresolution decomposition of the wavefield response dynamics obtains a nested subspace representation for the signal

$$S = V_0 \subset V_1 \subset \dots \subset V_P \dots \quad (6)$$

- 20 at increasingly high level of detail. Of course one is interested in a decomposition which is the least possible computationally expensive, that is the "smallest" representation subspace, for a "reasonable" approximation accuracy.

If the unknown channel variations are characterized statistically (for example using the well-known WSSUS, Wide Sense Stationary Uncorrelated Scattering assumption) S is not anymore a linear subspace but an ensemble of linear subspaces and it is possible to design a representation subspace that is close "on average" to S .

- 25 A measure of the distance between two closed subspaces S and V is the deviation $d(S,V)$ which is based on the concept of (constrained) Kolmogorov n width.

The deviation is a one-sided measure. That means that it addresses only the question of how well S is included in V but not vice versa, which is also an important issue. In fact, V may be too "large" to be of any practical interest. What a practical

implementation really needs is the "smallest" subspace that minimizes the deviation. A "small" subspace implies that the number of coefficients needed to represent the orthogonal projection is small, which results in less degrees of freedom, reduced sensitivity to noise and simplicity of computation. Since the subspace representation for S over a set of predetermined basis vectors indexed by the integer P (and for each P approximated by M) is of interest, the procedure is as follows:

1. find the deviation for each subspace with respect to S in the class of subspaces represented by Equation (6);
2. select the one (that is select the resolution depth P) that yields a tolerably small deviation; and
3. "shrink" the subspace retaining only part of the coefficients and select M in a way that the deviation is still close to the one selected in step 2.

If the unknown channel variations are characterized statistically, S is not anymore a linear subspace but an ensemble of linear subspaces. Statistical characteristics of the fading channel are typically available from experimental measurements in the form of a scattering function or autocorrelation function. This knowledge translates to the knowledge of the following correlations

$$E \{ g_{i1,i2}(n,k1) * g_{i3,i4}(n+m,k2) \} = R_{i1,i2,i3,i4}(m,k1,k2),$$

for any $i1,i2,i3,i4,m,k1,k2$.

The average deviation between S and V is

$$d(S,V)^2 = E_s - \text{Trace}[A^T P_A A R_h] \quad (7)$$

where

1. $\text{Trace}[]$ is the Trace operator for a matrix, that is the sum of the elements along the diagonal;
2. $A = I_K \otimes (I_{NR} \otimes s)$;
3. $P_A = B (B^T B)^{-1} B^T$ with $B = [d(0), d(1), \dots, d(NR-1)]$;
4. \otimes is the Kronecker product operator between two matrices (the element-wise product);
5. $*$ means complex conjugation for scalars, vectors and matrices;

6. $R_h = E\{h h^T\}$ with $h = [h_1(0)^T h_1(1)^T, \dots, h_1(NR-1)^T h_2(0)^T, \dots, h_2(NR-1)^T, h_k(0)^T, \dots, h_k(NR-1)^T]^T$; and

7. $E\{\}$ means statistical expectation.

Detailed and rigorous derivations that explain equation (7) are contained in
 5 Appendix 1 of Provisional Application No. 60/136,699, filed on May 28, 1999 incorporated herein by reference.

A technique to obtain the best values for P and M is then

1. Find the deviation for each subspace with respect to S in the class of subspaces represented by Equation (6) over the range $1 \leq p \leq P_{\max}$;
- 10 2. Select the smallest p such that $d(S, V_p)^2 - d(S, V_{p-1})^2 \leq \Delta$; and
3. "shrink" the subspace retaining UK (D+1) NR $(1 - \sum_{m=1,2,\dots,M} 2^{-m})$ coefficients in the formation of the function $L_N[d]$ for $M_{\min} \leq M \leq M_p$.

Observe that Δ is a preselected small number that determines the approximation accuracy of the representation subspace.

15 The algorithmic procedure to find the optimum P and M is detailed in the flow diagram of Figure 8.

F. Real-Time Implementation

There is a celebrated method known as the Viterbi algorithm (G. D. Forney, "Maximum Likelihood Sequence Estimation of Digital Sequences in the Presence of
 20 Intersymbol Interference," IEEE Trans. Inform. Theory, vol. IT-18, pp. 363-378, May 1972) that performs the task of minimizing $L_N[d]$ efficiently. The significance of the Viterbi algorithm is that the number of computations required for the detection of a sequence of length N grows only linearly with N. The Viterbi algorithm is well known to those skilled in the art of Maximum Likelihood Sequence Detection (or
 25 Estimation).

To apply the Viterbi algorithm one has to reduce the function $L_N[s]$ to a sum of terms where each term corresponds to the length of a branch in a suitable trellis (or tree) diagram. Also, one needs a real-time algorithm to compute the the estimated vector $w_k[P, M, d]$ in $L_N[d]$ on a sample by sample basis. This can be easily derived
 30 defining $w_{k,n}[P, M, d]$ as $w_k[P, M, d]$ estimated at time step n. Possible approaches are gradient-based methods (like the LMS, Least Mean Squares) and Recursive Least Squares-based (RLS) methods.

To reduce the function $L_N[d]$ to a sum of terms where each term corresponds to the length of a branch in a suitable trellis (or tree) diagram, it is convenient to define the variables:

$$F_n = [d(n)^T, d(n-1)^T, \dots, d(n-D)^T]^T \text{ for } n=D, D+1, \dots, NR$$

5 and the quantities:

$$G_{n+1}(F_D, \dots, F_{n+1}) = \sum_{k=1, \dots, K} \sum_{m=1, \dots, n} |y_k(m) - d(m)^T w_{k,m}[P, M, d]|^2$$

where $w_{k,m}[P, M, d]$ is recursively computed as:

$$w_{k,m}[P, M, d] = w_{k,m-1}[P, M, d] + \mu [y_k(m) - d(m)^T w_{k,m-1}[P, M, d]] d(m)^T \quad m=1, 2, \dots, n,$$

and the initialization is $w_{k,m}[P, M, d]=0$.

- 10 Observe that $G_{n+1}(F_D, \dots, F_{n+1})$ depends on $d(m)$, for $m=1, 2, \dots, n$, that is, on a path in the trellis.

Also, defining

$$J_{n+1}(F_n, F_{n+1}) = \sum_{k=1, \dots, K} |y_k(n) - d(n)^T w_{k,n}[P, M, d]|^2$$

- we see that $J_{n+1}(F_n, F_{n+1})$ depends on $d(n)$ and $d(n-1)$ only, that is, on a branch in the
15 trellis. It is easy to verify that:

$$G_{n+1}(F_D, \dots, F_{n+1}) = G_n(F_D, \dots, F_n) + J_{n+1}(F_n, F_{n+1}).$$

- There is a one-to-one correspondence between the sequence of transmitted symbols and the sequence of states F_D, \dots, F_{n+1} . Therefore the problem of selecting the most likely symbol-sequence is equivalent to that of selecting the most likely sequence
20 of states. The Maximum Likelihood detection problem has been reduced to the selection of a path through the trellis, once the branches joining states F_n and F_{n+1} have been assigned the values taken by the function $J_{n+1}(F_n, F_{n+1})$ usually referred as the branch metric. Any particular digital modulation scheme, with its own associated

alphabet, length D , and number of transmit antennas U will generate a different trellis structure. The minimum-metric path corresponds to the most likely sequence of states and hence to the most likely sequence of symbols. A summary of the necessary steps is given below. Step 1 Initialize: Let $n=D$, compute $G_D(F_D)$ for every possible value
 5 of F_D and store them.

Step 2 Extend survivor paths : Let $n=n+1$ and compute $J_{n+1}(F_n, F_{n+1})$ for each pair of states F_n, F_{n+1} such that the transition from F_n to F_{n+1} is allowed by the trellis structure. Step 3 Drop Paths: For each state F_{n+1} compute $u_{n+1}(F_{n+1})$ as the minimum over any F_n of $u_{n+1}(F_{n+1}) + J_{n+1}(F_n, F_{n+1})$ where $u_D(F_D) = G_D(F_D)$ by definition and
 10 $u_{n+1}(F_{n+1})$ is recursively computed. Step 4 Trace-back procedure. Step 5 Iterate: Go to Step 2 if not $n=N$.

The detected symbol is given at the output by means of the trace-back procedure, the procedure that outputs the estimated symbol as the one associated with the minimum euclidean distance path among the retained paths (also defined
 15 survivors).

G. Conclusion

The invention provides many advantages over known techniques. Advantages of the invention include the ability to communicate high data rates from one location to another, where the data rates are in excess of those conventionally achievable.

20 Having disclosed exemplary embodiments and the best mode, modifications and variations may be made to the disclosed embodiments while remaining within the scope of the invention as defined by the following claims.

CLAIMS

1. An apparatus for communicating information from one location to another through a wavefield space using a multi-dimensional communication protocol comprising:
 - 5 a transmitter configured to receive a message and to encode a plurality of signals associated with the message;
a first plurality of antennas coupled to the transmitter and configured to transmit the plurality of signals associated with the message;
a second plurality of antennas configured to receive the plurality of signals
 - 10 associated with the message; and
a receiver coupled to the second plurality of antennas and configured to decode the plurality of signals associated with the message to reconstruct the original information, wherein the receiver has no advance knowledge of at least one of the dimensions of the multi-dimensional protocol.
- 15 2. The apparatus of claim 1, wherein the protocol is at least a three-dimensional protocol and wherein:
 - the transmitter includes a plurality of transmit modules that each encode at least a portion of the message; and
 - the receiver includes a plurality of receiver modules that each decode
 - 20 complementary portions of the message to reconstruct the original information.
3. The apparatus of claim 1, wherein:
 - the receiver is configured to execute a statistical procedure to identify and decode the plurality of signals.
4. The apparatus of claim 3, wherein:
 - 25 the receiver is configured to execute a generalized likelihood detection procedure to identify the plurality of signals and then execute a maximum likelihood detection procedure to decode the plurality of signals.

5. The apparatus of claim 4, wherein
the receiver is configured to estimate the wavefield space using a virtual
wavefield space that approximates the wavefield space.
6. An apparatus for communicating information from one location to another
5 though a wavefield space using a multi-dimensional communication protocol
comprising:
a first transceiver configured to receive a message and to encode a plurality of
signals associated with the message;
a first plurality of antennas coupled to the first transceiver and configured to
10 transmit the plurality of signals associated with the message;
a second plurality of antennas configured to receive the plurality of signals
associated with the message; and
a second transceiver coupled to the second plurality of antennas and configured
to decode the plurality of signals associated with the message to reconstruct the
15 original information, wherein the second transceiver has no advance knowledge of at
least one of the dimensions of the multi-dimensional protocol.
7. The apparatus of claim 6, wherein the protocol is at least a three-dimensional
protocol and wherein:
the first transceiver includes a plurality of transmit modules that each encode at
20 least a portion of the message; and
the second transceiver includes a plurality of receiver modules that each
decode complementary portions of the message to reconstruct the original information.
8. The apparatus of claim 6, wherein:
the second transceiver is configured to execute a statistical procedure to
25 identify and decode the plurality of signals.
9. The apparatus of claim 8, wherein:
the second transceiver is configured to execute a generalized likelihood
detection procedure to identify the plurality of signals and then execute a maximum
likelihood detection procedure to decode the plurality of signals.

10. The apparatus of claim 9, wherein
the second transceiver is configured to estimate the wavefield space using a
virtual wavefield space that approximates the wavefield space.
11. A digital Wireless Transceiver comprising:
5 a digital circuit for detection of the U number of different signals after radio
frequency intermediate frequency downconversion comprised of digital baseband
downconversion, trellis search processor, vector symbol synchronizer, wavefield
estimator, wavefield gradient-based estimator, deinterleaver, channel decoder and data
extractor; and
10 a digital circuit for detection of the U number of different signals after radio
frequency intermediate frequency downconversion able to cope with and exploit
frequency selective multipath propagation, arbitrarily time-varying fading
characteristics, non Line-Of-Sight communication.
12. A method of communicating information from one location to another though
15 a wavefield space using a multi-dimensional communication protocol comprising the
steps of:
receiving a message at an input terminal;
encoding a plurality of signals associated with the message using an encoder;
transmitting the plurality of signals associated with the message using a first
20 plurality of antennas;
receiving the plurality of signals associated with the message using a second
plurality of antennas; and
decoding the plurality of signals associated with the message to reconstruct the
original information using a receiver, wherein the decoding step uses no advance
25 knowledge of at least one of the dimensions of the multi-dimensional protocol.
13. The method of claim 12, wherein:
the decoding step includes the step of executing a statistical procedure to
identify and decode the plurality of signals.

14. The method of claim 13, wherein:
the decoding step includes the step of executing a generalized likelihood detection procedure to identify the plurality of signals and then executing a maximum likelihood detection procedure to decode the plurality of signals.
- 5 15. The method of claim 14, wherein
the decoding step includes the step of estimating the wavefield space using a virtual wavefield space that approximates the wavefield space.
16. An apparatus for communicating information from one location to another through a wavefield space using a multi-dimensional communication protocol
- 10 comprising:
- means for receiving a message at an input terminal;
 - means for encoding a plurality of signals associated with the message;
 - means for transmitting the plurality of signals associated with the message;
 - means for receiving the plurality of signals associated with the message; and
 - 15 means for decoding the plurality of signals associated with the message to reconstruct the original information, wherein the means for decoding has no advance knowledge of at least one of the dimensions of the multi-dimensional protocol.

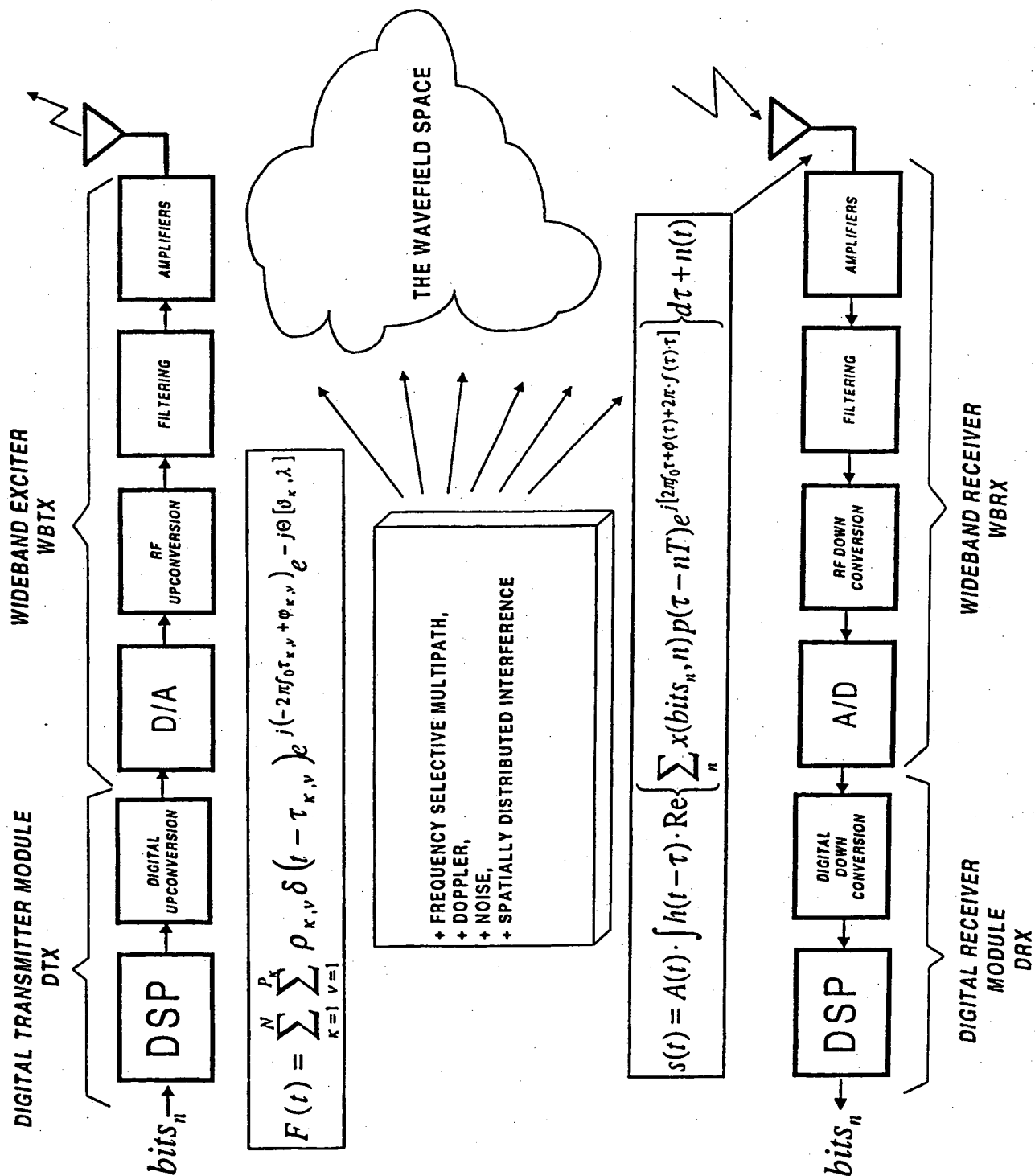


Figure 1A

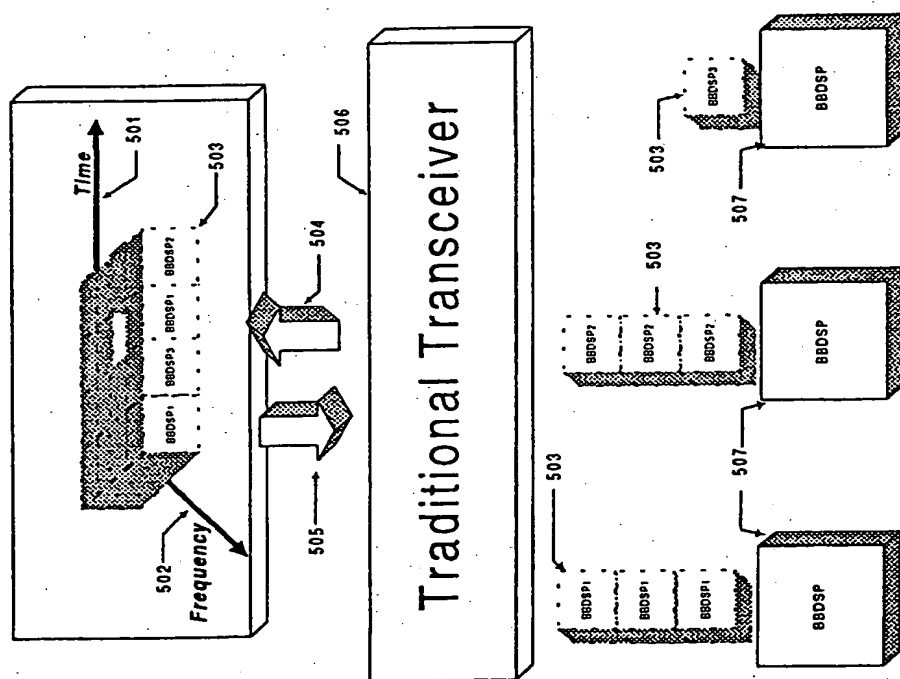


Figure 1B

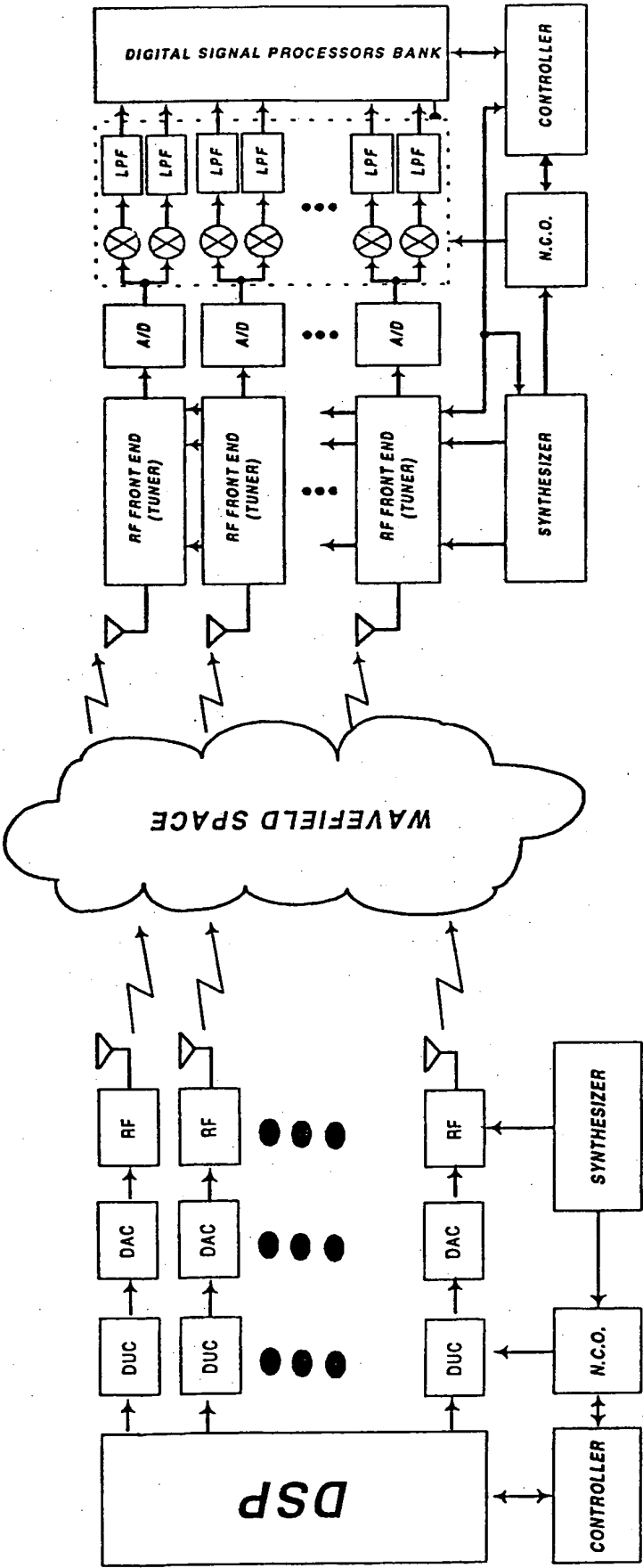


Figure 2A

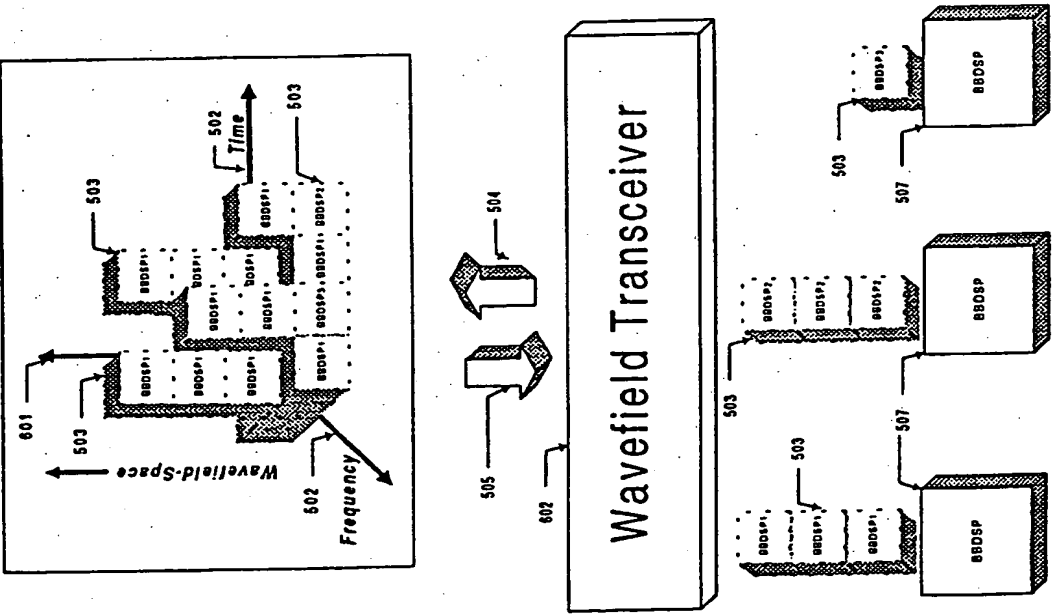
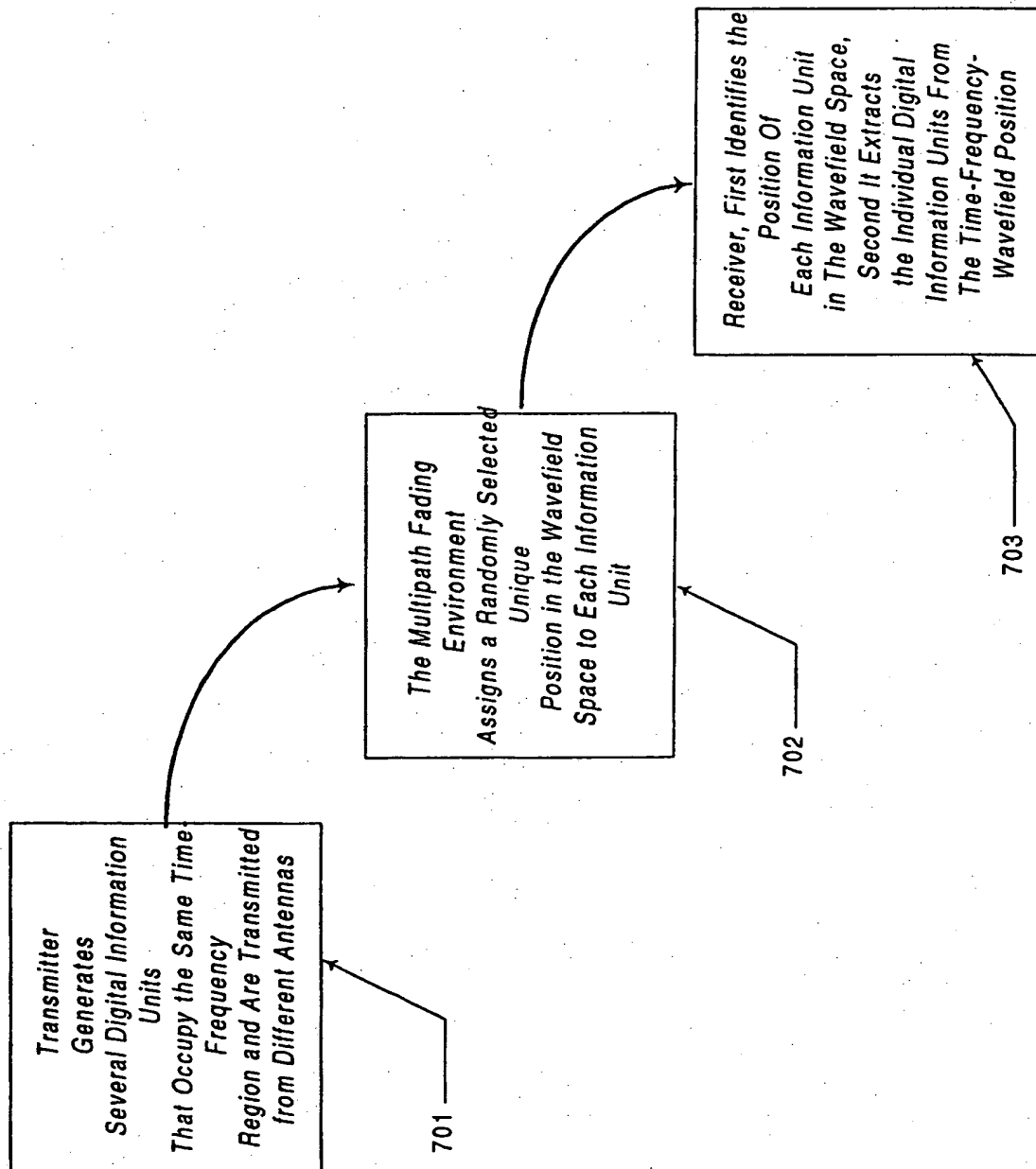


Figure 2B

**Figure 3**

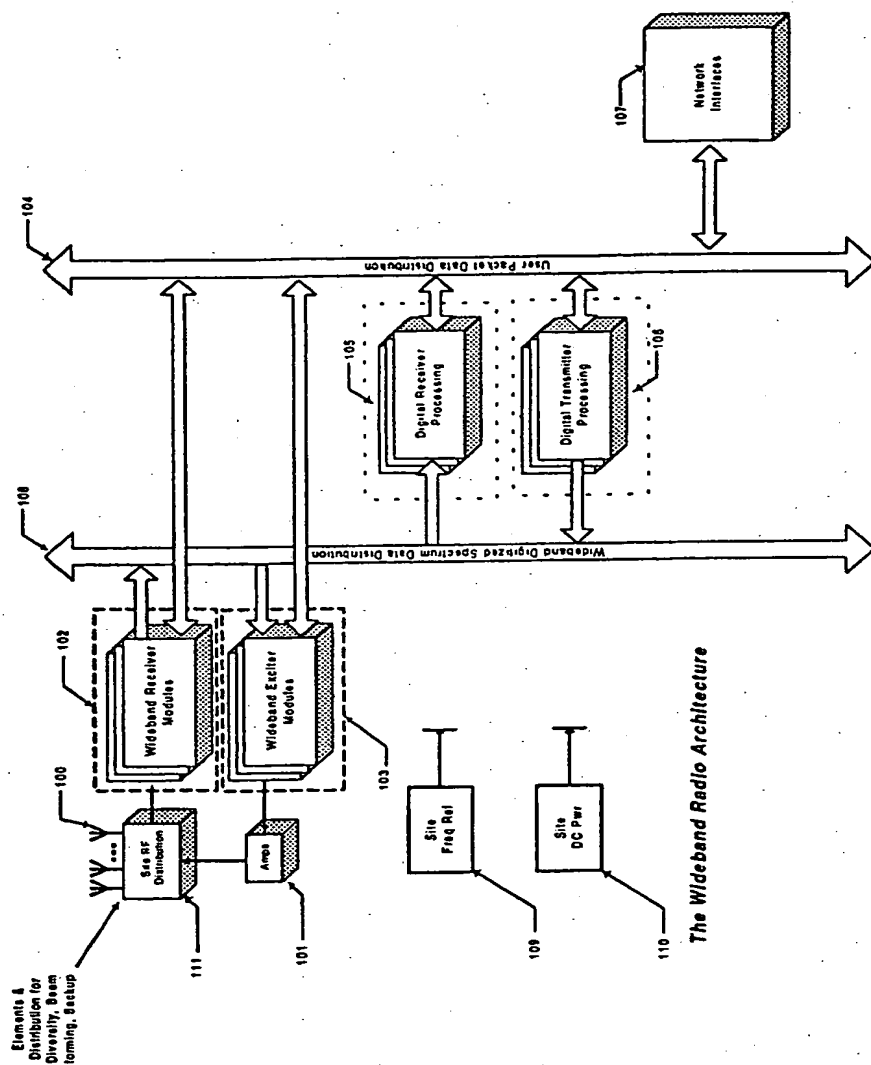


Figure 4

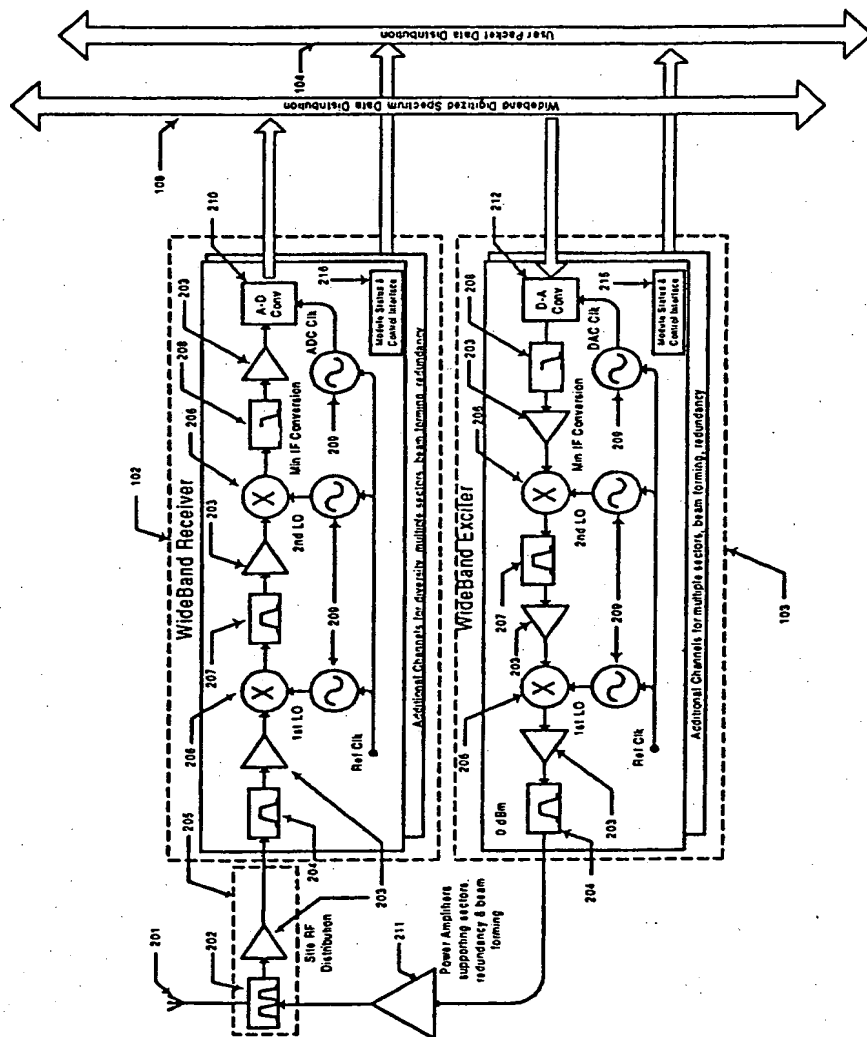


Figure 5

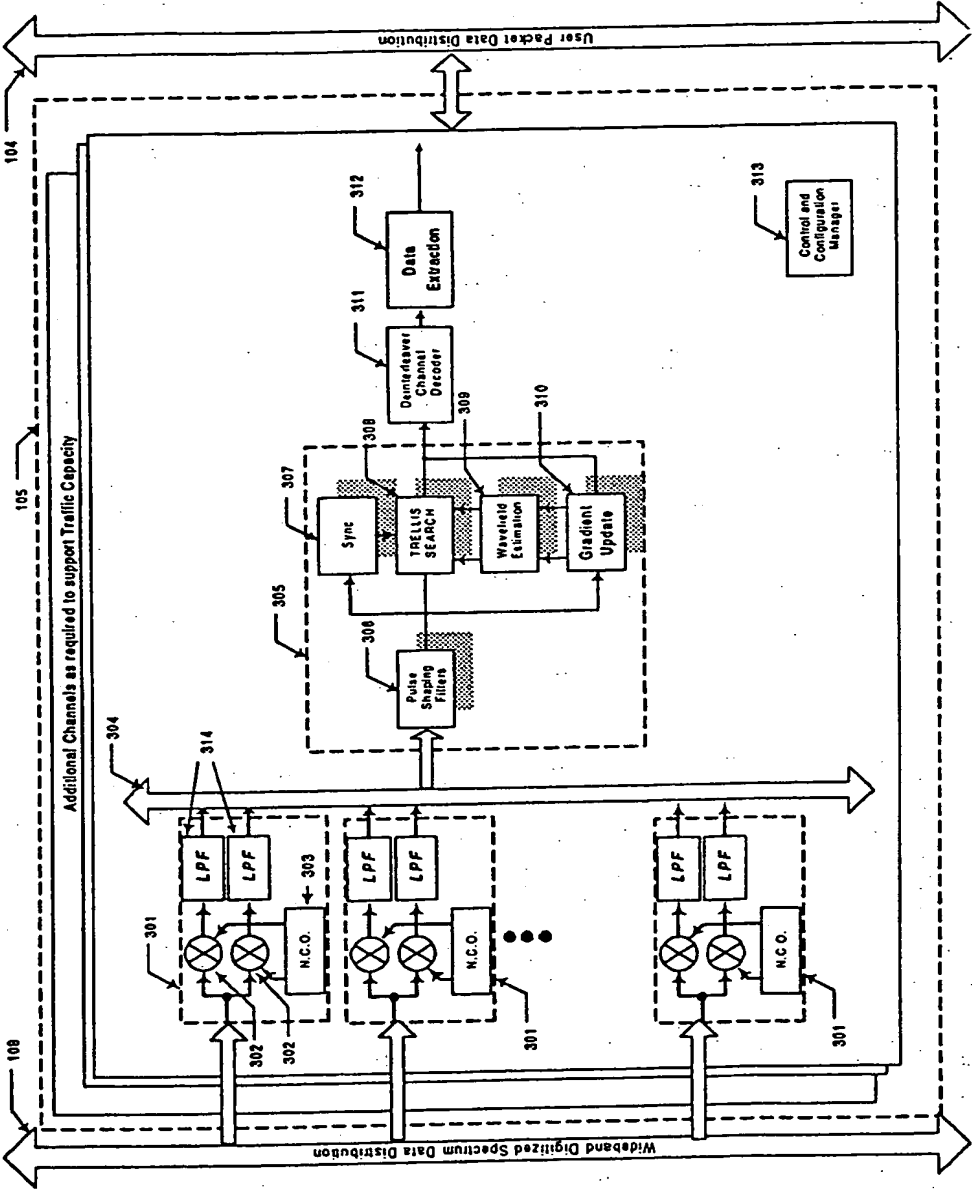


Figure 6

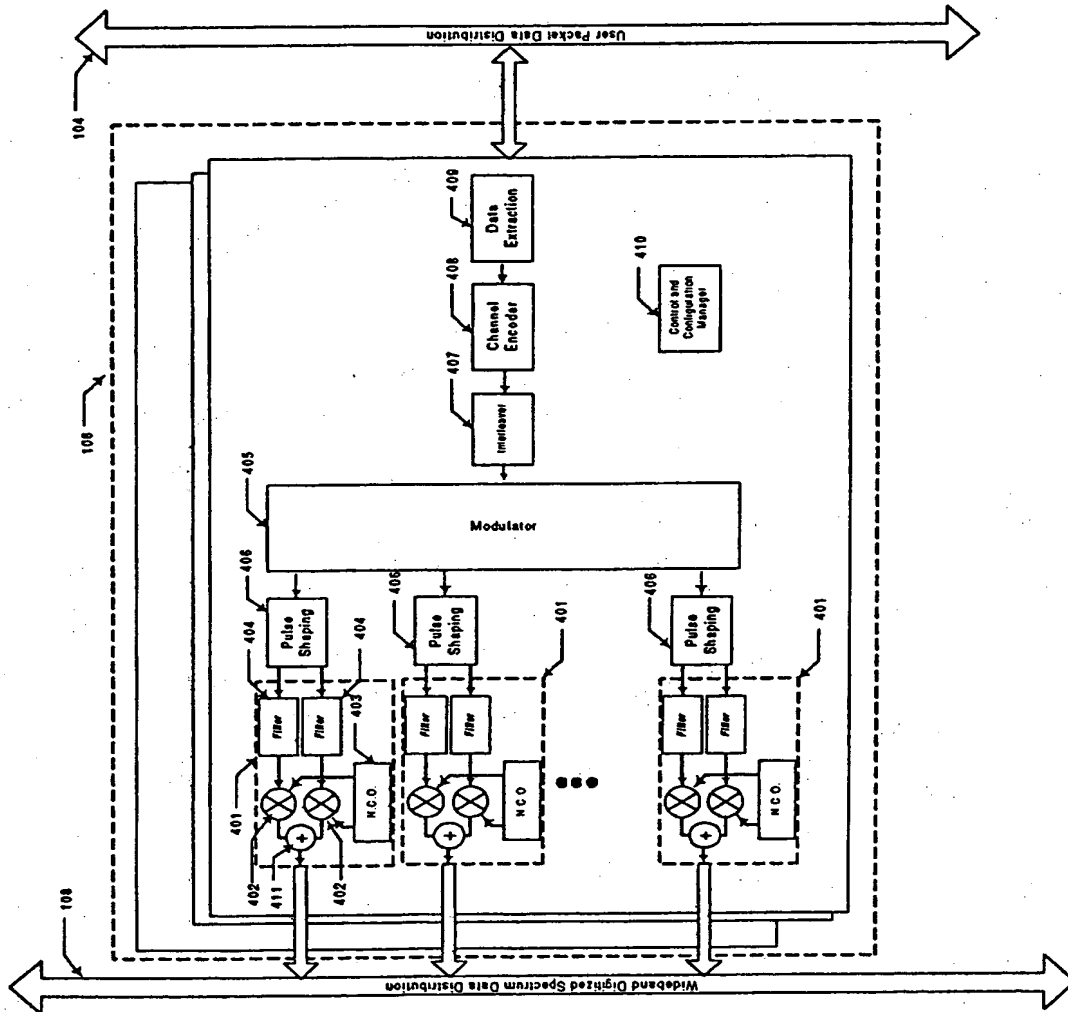
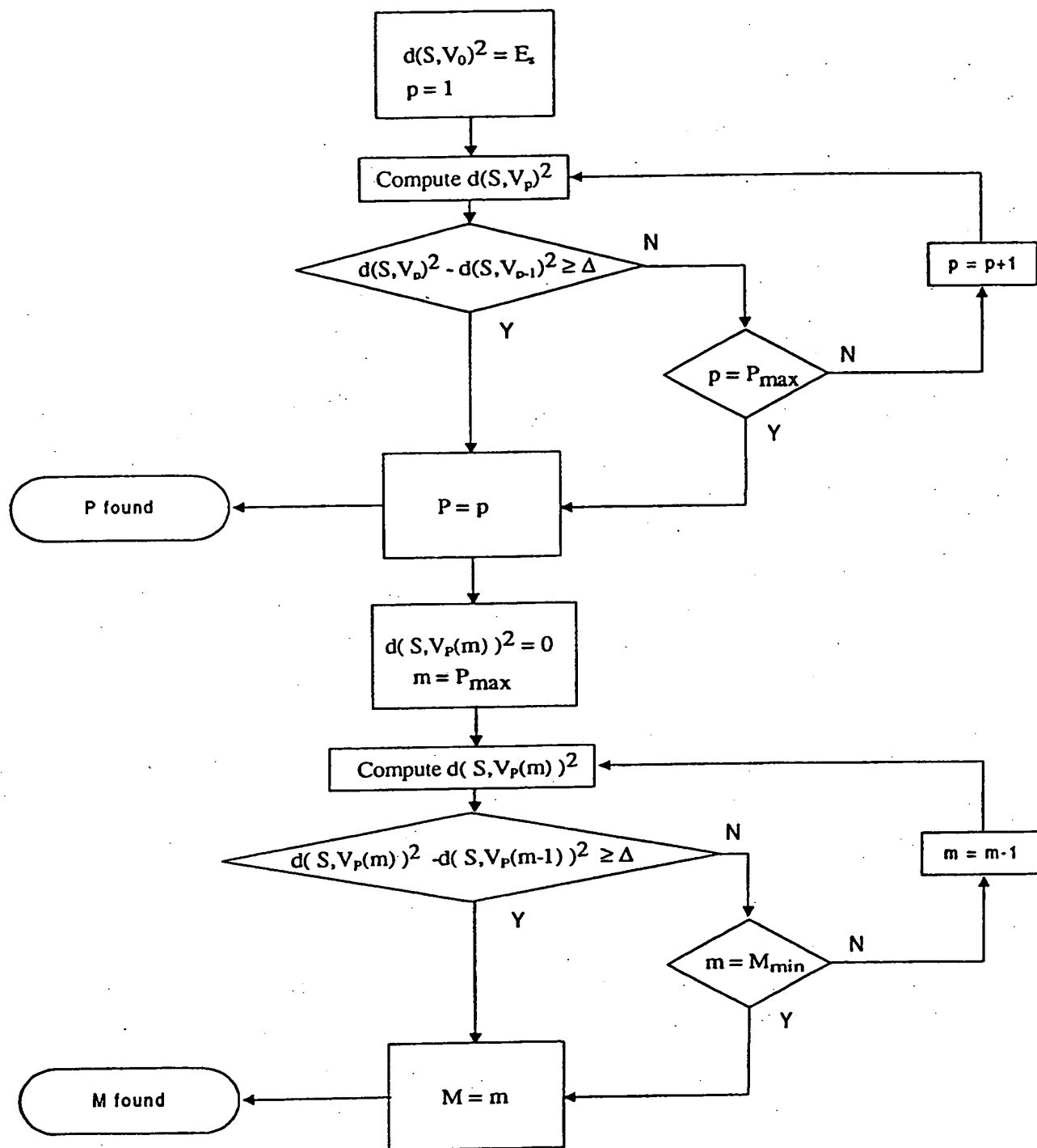


Figure 7

**Figure 8**

INTERNATIONAL SEARCH REPORT

International application No.
PCT/US00/12069

A. CLASSIFICATION OF SUBJECT MATTER

IPC(7) : H04B 7/02; H04L 27/06

US CL : 375/267, 340

According to International Patent Classification (IPC) or to both national classification and IPC

B. FIELDS SEARCHED

Minimum documentation searched (classification system followed by classification symbols)

U.S. : 375/267, 340, 260, 219, 341

Documentation searched other than minimum documentation to the extent that such documents are included in the fields searched
none

Electronic data base consulted during the international search (name of data base and, where practicable, search terms used)

EAST

Search terms: multi-dimensional protocol; transceiver, maximum likelihood, diversity

C. DOCUMENTS CONSIDERED TO BE RELEVANT

Category*	Citation of document, with indication, where appropriate, of the relevant passages	Relevant to claim No.
X	US 5,592,490 A (BARRATT et al) 07 January 1997, col. 6, line 55 - col. 7, line 58.	1-3,6-8,12, 13,16
X,P	US 5,960,039 A (MARTIN et al) 28 September 1999, col.3 line 47 - col. 4, line 65.	1-3,6-8,12, 13,16
X,P	US 6,058,105 A (HOCHWALD et al) 02 May 2000, col. 8 line 1 - col. 9 line 39.	1-3,6-8,12, 13,16
A	US 5,305,353 A (WEERACKODY) 19 April 1994, see abstract.	1,6,11-12, 16

☐ Further documents are listed in the continuation of Box C. ☐ See patent family annex.

* Special categories of cited documents:	*T	later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention
A document defining the general state of the art which is not considered to be of particular relevance	*X*	document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step when the document is taken alone
E earlier document published on or after the international filing date	*Y*	document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art
L document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)	*A*	document member of the same patent family
O document referring to an oral disclosure, use, exhibition or other means		
P document published prior to the international filing date but later than the priority date claimed		

Date of the actual completion of the international search

28 JUNE 2000

Date of mailing of the international search report

04 AUG 2000

Name and mailing address of the ISA/US
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INTERNATIONAL SEARCH REPORT

International application No.
PCT/US00/12069

Box I Observations where certain claims were found unsearchable (Continuation of item 1 of first sheet)

This international report has not been established in respect of certain claims under Article 17(2)(a) for the following reasons:

1. ☐ Claims Nos.:
because they relate to subject matter not required to be searched by this Authority, namely:

2. ☐ Claims Nos.:
because they relate to parts of the international application that do not comply with the prescribed requirements to such an extent that no meaningful international search can be carried out, specifically:

3. ☐ Claims Nos.:
because they are dependent claims and are not drafted in accordance with the second and third sentences of Rule 6.4(a).

Box II Observations where unity of invention is lacking (Continuation of item 2 of first sheet)

This International Searching Authority found multiple inventions in this international application, as follows:

Please See Extra Sheet.

1. ☒ As all required additional search fees were timely paid by the applicant, this international search report covers all searchable claims.
2. ☐ As all searchable claims could be searched without effort justifying an additional fee, this Authority did not invite payment of any additional fee.
3. ☐ As only some of the required additional search fees were timely paid by the applicant, this international search report covers only those claims for which fees were paid, specifically claims Nos.:

4. ☐ No required additional search fees were timely paid by the applicant. Consequently, this international search report is restricted to the invention first mentioned in the claims; it is covered by claims Nos.:

Remark on Protest

- ☐ The additional search fees were accompanied by the applicant's protest.
☐ No protest accompanied the payment of additional search fees.

INTERNATIONAL SEARCH REPORT

International application No.
PCT/US00/12069

BOX II. OBSERVATIONS WHERE UNITY OF INVENTION WAS LACKING

This ISA found multiple inventions as follows:

This application contains the following inventions or groups of inventions which are not so linked as to form a single inventive concept under PCT Rule 13.1. In order for all inventions to be searched, the appropriate additional search fees must be paid.

Group I, claims 1-10 and 12-16 are, drawn to multi-dimensional communication protocol.

Group II, claim(s) 11 is, drawn to digital wireless transceiver.

The inventions listed as Groups I and II do not relate to a single inventive concept under PCT Rule 13.1 because, under PCT Rule 13.2, they lack the same or corresponding special technical features for the following reasons: Group I is directed to a multi-dimensional communication protocol and Group II is directed to a digital wireless transceiver for detecting different signals.